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3.

⋮

(1) $\min F_1(u),$

(2) $\min F_2(u),$

(3) $\max F_3(u),$

$F_1, F_2 -$

$, F_3 -$

()

(4) $u = \{u_i^j, i = 1, \dots, 4, j = 1, \dots, J_i\}.$

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(), $\langle i \rangle,$

$\langle j \rangle.$

(5) $F_1(u) = \frac{T}{C(u)} \left(u_\Sigma^0 + \frac{u_1 + P(u) - C(u)}{2} \right), u_\Sigma^0 = \sum_{i=1}^3 u_i^0,$

(6) $F_2(u) = F_1(u) + \frac{T}{R(u)} \left(u_4^0 + \frac{R(u) - g(u)}{2} \right),$

(7) $F_3(u) = R(u) - C(u),$

- (); $u_i^0, i = 1, \dots, 4$ -

() , , ; R, - ,

() ; - -

); g –

(5), (6)

u_1 ,

(1)-(3)

u_1 .

$$P(u_1), P'_{u_1}(u_1) > 0,$$

$$C(u_1), C'_{u_1}(u_1) > 0,$$

$$R(u_1), R'_{u_1}(u_1) > 0,$$

$$g(u_1), g'_{u_1}(u_1) > 0.$$

$$(8) P(u_1) = B_P u_1^{S_P}, B_P > 0, 0 < S_P < 2,$$

$$(9) C(u_1) = B_C u_1^{S_C}, B_C > 0, 0 < S_C < 2,$$

$$(10) R(u_1) = B_R u_1^{S_R}, B_R > 0, 0 < S_R < 2,$$

$$(11) g(u_1) = B_g u_1^{S_g}, B_g > 0, 0 < S_g < 2,$$

$$B_C, B_P, B_R, B_g, S_C, S_P, S_R, S_g -$$

$$0 < S < 2$$

[2].

(8)-(11)

u_1 ,

(4),

$$, \quad z_{j_1} = z_{j_1}(u_{1j_1}), j_1 = 1, \dots, J_1, z'_{j_1} < 0,$$

$$(12) \quad z_{j_1}(u_{1j_1}) = A_{z_{j_1}} u_1^{\Gamma_{z_{j_1}}}, \Gamma_{z_{j_1}} < 0, j_1 = 1, \dots, J_1,$$

$$A_{z_{j_1}}, \Gamma_{z_{j_1}} -$$

.

:

$$(13) \quad \sum_{j_1=1}^{J_1} \left[z_{j_1} \sum_{j_3=1}^{J_3} m_{j_1 j_3} \left(N_{j_3}^{\max(\min)} - u_{3j_3}^0 - k_{j_3} \cdot u_{2j_3}^0 \right) \right],$$

$$m_{j_1 j_3} -$$

$$j_1 -$$

$$j_3 -$$

$$; N_{j_3}^{\max(\min)} -$$

$$j_3 -$$

$$; k_{j_3} -$$

$$j_3 -$$

$$; z_{j_1} -$$

$$j_1 -$$

(

).

$$(14) \quad u_1 \geq u_1^{\min}(z),$$

$$u_1$$

$$(12).$$

$$(15) \quad u_{1(1)}^* = \arg \min_{u_1 \in U} F_1(u_1),$$

$$(16) \quad u_{1(2)}^* = \arg \min_{u_1 \in U} F_2(u_1),$$

$$(17) u_{1(3)}^* = \arg \max_{u_1 \in U} F_3(u_1),$$

$$(18) U = \left\{ u_1 \in R^+ \mid u_1^{\max}(N) \geq u_1 \geq u_1^{\min}(N), u_1 \geq u_1^{\min}(z) \right\},$$

4.

(14)

$$(19) P_{\Sigma}(u) = \sum_{j_1=1}^{J_1} z_{j_1} (u_{1j_1}) u_{1j_1} + P(u_1).$$

1:

$$(19) \quad (8), (12)$$

$$u_{1j_1}^{\min} \geq 0$$

$$(20) u_{1j_1}^{\min}(z) = \left(\frac{B_p S_p}{-(r_{z_{j_1}} + 1) A_{z_{j_1}}} \right)^{\frac{1}{r_{z_{j_1}}}} \left(\sum_{j_1=1}^{J_1} u_{1j_1}^{\min}(z) \right)^{\frac{S_p-1}{r_{z_{j_1}}}},$$

$$j_1 = 1, \dots, J_1$$

$$S_p \leq 1 \cap r_{z_{j_1}} < -1 \cap A_{z_{j_1}} (r_{z_{j_1}} + 1) r_{z_{j_1}} u_{1j_1}^{r_{z_{j_1}}-1} >$$

$$(21) B_p S_p | S_p - 1 \left(\sum_{j_1=1}^{J_1} u_{1j_1} \right)^{S_p-2} .$$

$$(21)$$

$$(r_{z_{j_1}} < -1).$$

$$(14)$$

$$(|r_{z_{j_1}}| < 1),$$

$$u_{1j_1}^{\min} < 0.$$

$$(21)$$

$$(S_p \leq 1).$$

$$\bar{r}_z, \bar{A}_z, \bar{u}_1^{\min}); \quad (20)$$

$$(22) \bar{u}_1^{\min}(z) = \left(-\frac{B_p S_p J_1^{S_p-1}}{(\bar{r}_z + 1) \bar{A}_z} \right)^{\frac{1}{\bar{r}_z - S_p - 1}}.$$

$$(1)-(3) \quad (18),$$

$$u_{1F1}^*, u_{1F2}^*, u_{1F3}^*.$$

$$(8), (9)$$

$$(23) S_p < S_C + 1,$$

$$(S_p > S_C + 1)$$

$$(10), (11)$$

$$(24) S_g < S_R + 1,$$

$$(S_g > S_R + 1)$$

$$(5) \quad (8), (9) \quad (23)$$

$$u_{1F1}^* \geq 0, \quad -$$

$$(25) \quad -2u_{\Sigma}^0 S + (1-S) u_{1F1}^* + B_P (S_P - S_C) u_{1F1}^{*SP} = 0$$

$$(26) \quad u_{1F1}^* \in U_1 = \left\{ \begin{array}{l} S_C > S_P \cup S_C < S_P \cap S_C + 1 > S_P \cap \\ \{ (S_C, S_P, u_{\Sigma}^0, u_1) > 0 \} \end{array} \right\},$$

$$\{ (S_C, S_P, u_{\Sigma}^0, u_1) = S_C [2(S_C + 1)u_{\Sigma}^0 + S_C - 1] u_1 + B_P |S_C - S_P| (S_C + 1 - S_P) u_1^{SP} \}$$

$$(25)$$

$$u_{1F1}^* \geq 0:$$

$$(27) \quad u_{1F1}^* = \left(\frac{2u_{\Sigma}^0 S_C}{B_P (S_P - S_C)} \right)^{1/S_P} \quad \forall S_C \approx 1, \quad S_P > S_C,$$

$$(28) \quad u_{1F1}^* = \frac{2u_{\Sigma}^0 S_C}{1 - S_C} \quad \forall S_C \approx S_P, \quad S_C < 1,$$

$$(29) \quad u_{1F1}^* = \frac{2u_{\Sigma}^0 S_C}{1 - S_C + B_P (S_P - S_C)} \quad \forall S_P \approx 1, \quad S_C < \frac{1 + B_P S_P}{1 + B_P},$$

$$(30) \quad u_{1F1}^* = \frac{2u_{\Sigma}^0 S_C - B_P (S_P - S_C)}{1 - S_C} \quad \forall S_P \ll 1, \quad S_C < 1.$$

$$(27), \quad -$$

$$(S_P > S_C), \quad -$$

$$(S_C \approx 1),$$

;

$$(28),$$

$$(S_C < 1),$$

$$(S_P \approx S_C)$$

$$(\quad - \quad). \quad (29),$$

$$S_C < 1,$$

$$S_P < 1,$$

$$(28),$$

$$(S_P \approx 1). \quad , \quad (30)$$

$$(\quad , \quad)$$

),

$$(S_P \ll 1);$$

$$(30)$$

$$S_C < 1.$$

$$(27)-(30)$$

$$(27)-(30)$$

$$u_{\Sigma}^0,$$

$$u_{1F1}^* \gg u_1^0,$$

$$\begin{aligned}
& u_{\Sigma}^0, & u_{1F1}^* \\
& s_C, s_P \\
s_C [2(s_C + 1)u_{\Sigma}^0 + s_C - 1] u_1 \gg B_p |s_C - s_P| (s_C + 1 - s_P) u_1^{sp}, \\
(26)
\end{aligned}$$

$$(31) \quad \left\{ \begin{aligned} & u_{1F1}^* \geq 0, \\ & (s_C, s_P, u_{\Sigma}^0, u_1) > 0 \forall u_{1F1}^* \geq 0. \end{aligned} \right.$$

(31)

$$\begin{aligned}
& 3: \\
(6) \quad & (8)-(11) \quad (23), (24) \\
& u_{1F2}^* \geq 0,
\end{aligned}$$

$$\begin{aligned}
(32) \quad & -s_C \frac{u_{\Sigma}^0}{B_c} + \frac{1-s_C}{2B_c} u_{1F2}^* + \frac{B_p}{2B_c} (s_P - s_C) u_{1F2}^{*sp} - \\
& s_R \frac{u_4^0}{B_R} u_{1F2}^{*-s_R+s_C} - \frac{B_g}{2B_R} (s_g - s_R) u_{1F2}^{*s_g-s_R+s_C} = 0
\end{aligned}$$

(33)

$$\begin{aligned}
& u_{1F2}^* \in U_2 = \\
& \left\{ \begin{aligned} & (s_g > s_R \cap s_g < s_R + 1) \forall u_{1F2}^*, \\ & s_g \leq s_R \cap \left\{ (s_C, s_P, u_{\Sigma}^0, u_{1F2}^*) + s_R (s_R + 1) \frac{u_4^0}{B_R} u_{1F2}^{*-s_R-2} + \right. \\ & \left. \frac{B_g}{2B_R} (s_g - s_R) (s_R + 1 - s_g) u_{1F2}^{*s_g-s_R-2} > 0. \right. \end{aligned} \right. \\
& (32)
\end{aligned}$$

:

$$(34) \quad u_{1F2}^* = \frac{2(B_R S_C u_{\Sigma}^0 + B_C S_R u_4^0)}{B_g B_C (S_g - S_R) - B_R (1 - S_C) - B_P B_R (S_P - S_C)},$$

$$\forall S_P \approx 1 \cap S_C \approx 1 \cap S_R \approx S_C \cap S_R \approx S_g$$

$$(35) \quad u_{1F2}^* = \frac{2(B_R S_C u_{\Sigma}^0 + B_C S_R u_4^0) - B_P B_R (S_P - S_C)}{B_R (1 - S_C) - B_g B_C (S_g - S_R)} \forall$$

$$S_P \ll 1 \cap S_C \approx S_R \cap S_g \approx 1$$

(34), (35),

$$u_{1F2}^* \geq 0, \quad (35)$$

$$S_P < S_C)$$

$$(34) \quad B_g B_C (S_g - S_R) - B_R (1 - S_C) - B_P B_R (S_P - S_C) > 0,$$

$$(35) \quad B_R (1 - S_C) - B_g B_C (S_g - S_R) > 0.$$

(35)

$$(S_C < 1)$$

$$(S_R > S_g),$$

$$S_R < S_g,$$

$$B_R (1 - S_C) > B_g B_C |S_g - S_R|. \quad (34)$$

$$: \quad S_C > 1$$

$$S_R < S_g,$$

$$S_C < 1$$

$$B_P B_R (S_P - S_C) > B_g B_C (S_g - S_R) + B_R (1 - S_C).$$

(34)

$$(27), (28)$$

$$(S_C \approx 1)$$

$$(S_P \approx S_C \approx 1)$$

,

$$(S_R \approx S_C);$$

$$S_R \approx S_g. \quad (35)$$

$$(30), S_P \ll 1),$$

$$(S_R \approx S_C),$$

$$(S_R < S_C),$$

$$(S_R > S_C);$$

$$(S_g \approx 1),$$

$$(34),(35)$$

$$u_{\Sigma}^0 + u_4^0,$$

$$u_{1F2}^*$$

$$(33)$$

$$(S_R < S_g < S_R + 1),$$

$$(S_g \leq S_R)$$

$$S_P \approx S_C \approx 1, S_R \approx S_g \approx 1,$$

$$S_C(S_C - 1)[2u_{\Sigma}^0 + u_{1F2}^*] + B_P(S_P - S_C)(S_P - S_C - 1)u_{1F2}^* + \\ + S_R(S_R + 1)\frac{u_4^0}{B_R}u_{1F2}^{*-3} - \frac{B_g}{2B_R}(S_g - S_R)(S_g - S_R - 1)u_{1F2}^{*-2} > 0,$$

$$\begin{aligned}
& , \\
u_4^0 & \cong u_{1F2}^*, u_{1F2}^{*-2} \ll u_{1F2}^* , \\
u_{1F2}^* & > - \frac{S_C(S_C-1)2u_\Sigma^0}{S_C(S_C-1) + B_P(S_P - S_C)(S_P - S_C - 1)} , \\
& , \\
& (26) (S_C > 1, S_P < S_C) \\
& u_{1F2}^* \geq 0 . \\
& 4: \qquad \qquad \qquad (7) \qquad \qquad \qquad (9),
\end{aligned}$$

$$\begin{aligned}
(10) \\
u_{1F3}^* & \geq 0,
\end{aligned}$$

$$(36) \quad u_{1F3}^* = \left(\frac{B_R S_R}{B_C S_C} \right)^{\frac{S_R-1}{S_C-1}} ,$$

(37)

$$u_{1F3}^* \in U_3 = \left\{ \begin{array}{l} S_C > 1 \cap \left[\left(S_R > 1 \cap \frac{B_R(S_R-1)S_R}{B_C(S_C-1)S_C} < u_{1F3}^{\frac{S_C-2}{S_R-2}} \right) \right. \\ \qquad \qquad \qquad \left. \cup (S_R < 1 \forall \cap u_{1F3}^* > 0) \right] \\ S_C < 1 \cap \left[S_R < 1 \cap \frac{B_R(S_R-1)S_R}{B_C(S_C-1)S_C} > u_{1F3}^{\frac{S_C-2}{S_R-2}} \right] \\ \cup [S_C < 1 \cap S_R > 1] \end{array} \right. ,$$

$$\begin{aligned}
& , \\
& u_{1F3}^* \\
& B_R, S_R
\end{aligned}$$

$$B_C, S_C.$$

$$: \quad (27)-(30) \quad ,$$

$$S_C$$

$$, \quad B_C, B_R, S_R$$

$$, \quad S_C; \quad (34), (35)$$

$$S_R (\quad u_{\Sigma}^0 \gg u_4^0),$$

$$S_C.$$

$$(36)$$

$$B_R, B_C \quad S_R, S_C$$

$$u_{1F3}^*$$

$$S_C < 1,$$

$$u_{1F3}^* \geq 0, \quad (37)$$

$$(S_R < 1),$$

$$u_{1F3}^* > \frac{B_R (S_R - 1) S_R}{B_C (S_C - 1) S_C},$$

$$\frac{S_C - 2}{S_R - 2} \approx 1, \quad \frac{B_R (S_R - 1) S_R}{B_C (S_C - 1) S_C} \approx 1,$$

$$(37), \quad S_C < 1 \quad u_{1F3}^*,$$

$$(38) u_{1(k)}^* = \max \left\{ \begin{array}{l} \min \{ u_{1Fk}^*, u_1^{\min}(N), u_1^{\min}(z) \}, \\ u_1^{\max}(N) \end{array} \right\}, k = 1, 2, 3$$

(15)-(17)

(18),

$$(39) U_k \cap U \neq \emptyset, k = 1, 2, 3.$$

5.

$$(8)-(11)$$

« [12] »
 2011-2013 .

$$u_i(t), i = 1, \dots, 3 \quad P(t), C(t), R(t), g(t)$$

(t -)

(1),

([11])

(0,7)

$$u_2 \quad u_1, u_3 \quad u_2,$$

$$(15)-(18),$$

$$P, C, R, g \quad u_3.$$

(8)-(11)

:

$$(40) \quad u_3(u_2) = A_{u_3} u_2^{\Gamma_{u_3}}, \quad u_2(u_1) = A_{u_2} u_1^{\Gamma_{u_2}}, \quad P(u_3) = A_P u_3^{\Gamma_P},$$

$$C(u_3) = A_C u_3^{\Gamma_C}, \quad g(u_4) = A_g u_4^{\Gamma_g}, \quad R(u_3) = A_{u_4} u_3^{\Gamma_{u_4}}$$

(40)

0,9). (40)

(15)-(18),

:

$$B_{T(k)} = B_{t(k)} \cdot 4^{1-S_{t(k)}} \quad (k = P, C, R, g, \quad \ll T \gg)$$

$$(41) \quad P(u_1) = 8585u_1^{0,3}, \quad C(u_1) = 45u_1^{0,76}, \quad g(u_1) = 144u_1^{0,7},$$

$$R(u_1) = 151u_1^{0,7}$$

I –

	u1	u2	u3	R (u4)	C	P	g
u1		0,80	0,35	0,51	0,35	0,06	0,51
u2			0,71	0,68	0,62	0,30	0,61
u3				0,89	0,93	0,77	0,83
R (u4)					0,93	0,69	0,94
C						0,71	0,89
P							0,61
g							

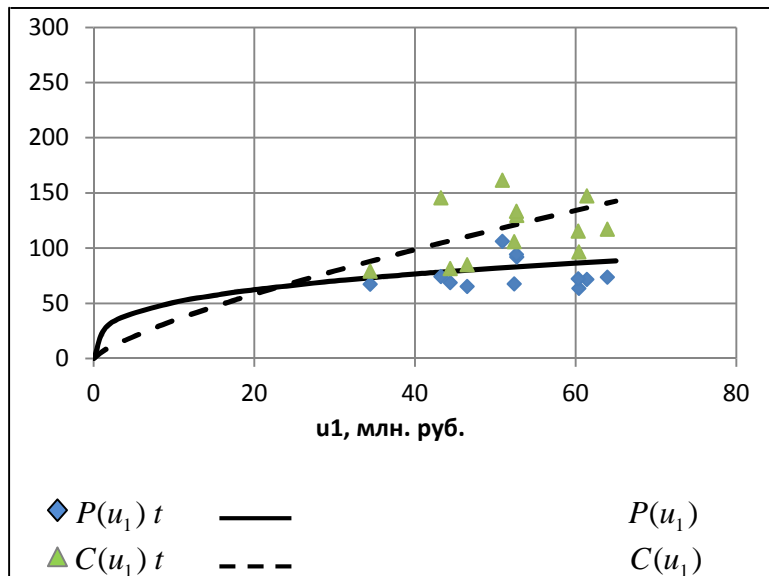
(12)

:

$$(42) \quad z_1(u_1^1) = 205u_1^{-0.3}, \quad z_2(u_1^2) = 105u_1^{-0.2}$$

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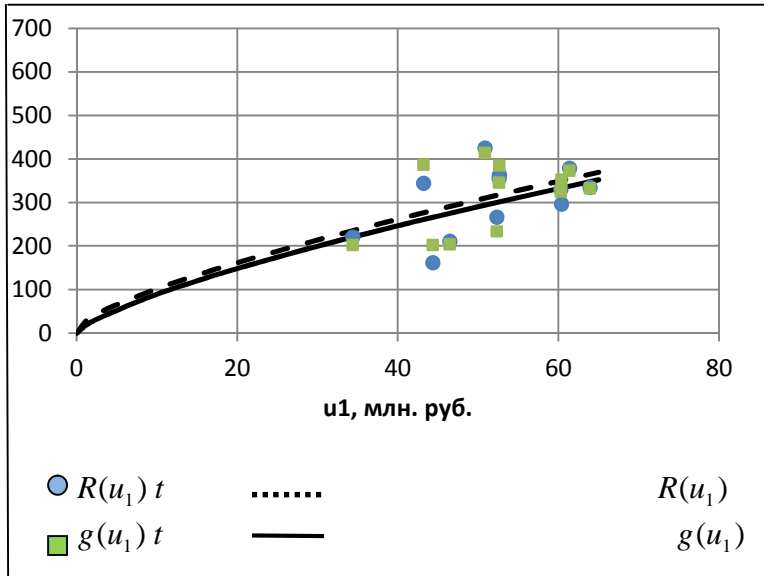
(41),(42),



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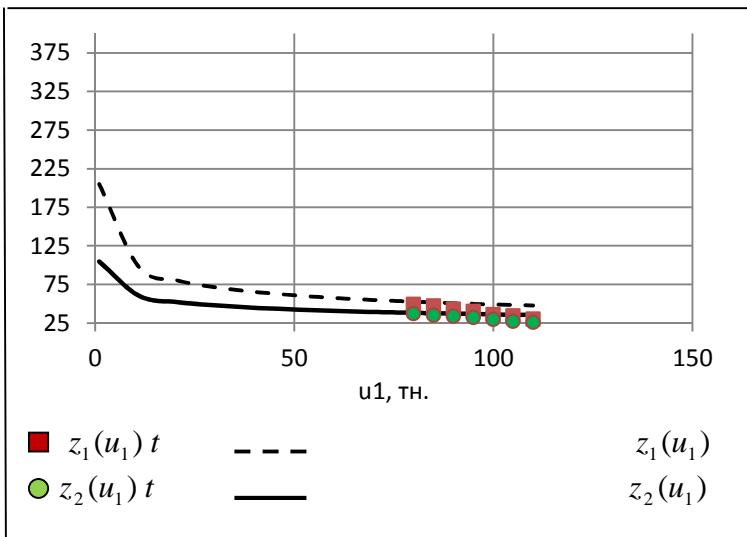
2011- 2013 ., . . .

(3).



.2.

2011-2013



.3.

« » 2011- 2013 . .

(41)

$$(43) \quad P(u_1) = 8585u_1^{0,3}, \quad C(u_1) = 45u_1^{0,76}, \quad g(u_1) = 144u_1^{0,7}, \\ R(u_1) = 151u_1^{0,7}$$

2 – (15)

u_{Σ}^0	$S_P = 1, S_C = 0,93$			$S_P = 1, S_C = 0,95$		
	$u_{1F1}^*(25)$	$u_{1F1}^*(27)$	$\Delta, \%$	$u_{1F1}^*(25)$	$u_{1F1}^*(27)$	$\Delta, \%$
100 000	91 626	94 898	3,57%	131 034	135 714	3,57%
200 000	183 251	189 796	3,57%	262 069	271 429	3,57%
300 000	274 877	284 694	3,57%	393 103	407 143	3,57%
u_{Σ}^0	$S_P = 0,45, S_C = 0,35$			$S_P = 0,4, S_C = 0,3$		
	$u_{1F1}^*(25)$	$u_{1F1}^*(28)$	$\Delta, \%$	$u_{1F1}^*(25)$	$u_{1F1}^*(28)$	$\Delta, \%$
100 000	106 903	107 692	0,74%	85 339	85 714	0,44%
200 000	214 305	215 385	0,50%	170 933	171 429	0,29%
300 000	321 781	323 077	0,40%	256 560	257 143	0,23%
u_{Σ}^0	$S_P = 0,88, S_C = 0,7$			$S_P = 0,9, S_C = 0,75$		
	$u_{1F1}^*(25)$	$u_{1F1}^*(29)$	$\Delta, \%$	$u_{1F1}^*(25)$	$u_{1F1}^*(29)$	$\Delta, \%$
100 000	88 329	104 869	18,73 %	94 605	101 124	6,89%

200 000	190 220	209 738	10,26 %	201 581	202 247	0,33%
300 000	297 739	314 607	5,67%	313 657	303 371	-3,28%

2

(27)-(29),

$$u_{1F1}^* (\quad . \quad) \quad \Delta (\%)$$

(25). (27)-

(29) , -

$$u_{\Sigma}^0 (\quad . \quad)$$

S_C , 18,73%

(30) , -

$$u_{1F1}^* \quad -$$

3 – (16)

u_{Σ}^0	u_4^0	$S_P = 0,96, S_C = 0,83,$ $S_R = 0,78, S_g = 0,83$			$S_P = 1, S_C = 0,92,$ $S_R = 0,9, S_g = 0,9$		
		$u_{1F1}^* (32)$	$u_{1F1}^* (34)$	$\Delta, \%$	$u_{1F1}^* (32)$	$u_{1F1}^* (34)$	$\Delta, \%$
100 000	50 000	100 092	83 230	- 16,85%	94 241	91 184	-3,24%
200 000	100 000	204 944	166 461	- 18,78%	188 900	182 368	-3,46%
300 000	200 000	334 820	260 156	- 22,30%	299 048	285 426	-4,56%

u_{Σ}^0	u_4^0	$S_P = 0,1, S_C = 1,25,$ $S_R = 0,9, S_g = 0,8$			$S_P = 0,05, S_C = 1,1,$ $S_R = 0,99, S_g = 0,91$		
		$u_{1F1}^* (32)$	$u_{1F1}^* (35)$	$\Delta, \%$	$u_{1F1}^* (32)$	$u_{1F1}^* (35)$	$\Delta, \%$
100 000	50 000	106 527	130 029	22,06%	110 116	106 710	-3,09%
200 000	100 000	237 021	260 042	9,71%	222 815	213 407	-4,22%
300 000	200 000	519 236	402 960	- 22,39%	378 115	333 022	- 11,93%

3

(34)-(35),

$u_{1F1}^* (\quad . \quad)$ $\Delta (\%)$
(32). (34)-

(35)

$u_{\Sigma}^0 (\quad . \quad)$ u_4^0 -
 S_C , 22,39%

. 4

$F_2(u_1)$, (6) (41)

$F_3(u_1)$ (7), $F_1(u_1)$ -

$F_2(u_1)$ -

- ; (13)

$u_1^{\min}(N)$, (14), (42),

(21) ;

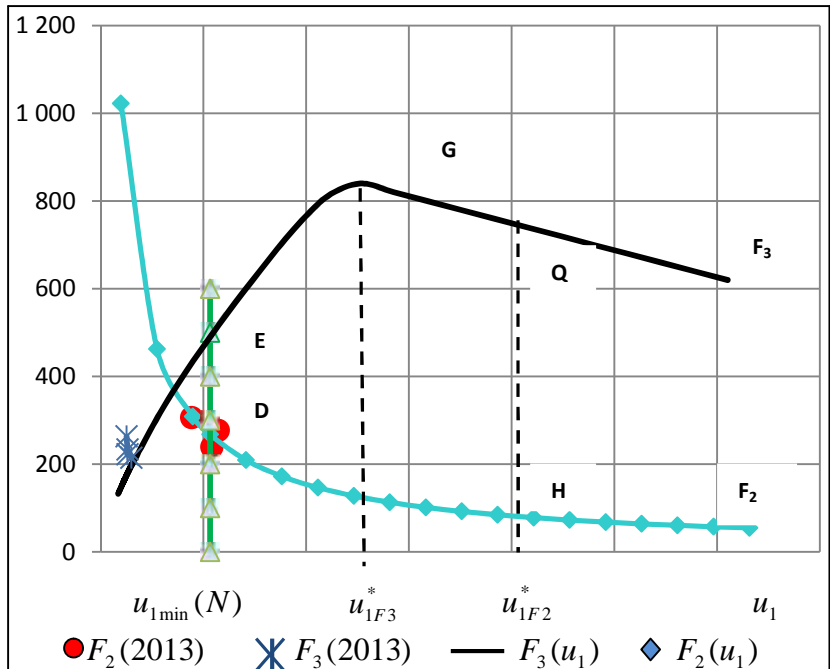
F_2, F_3 , -

2013 . , , -

$$u_{1F3}^* < u_{1F2}^*,$$

$$u_1 \in [u_1^{\min}(N), u_{1F3}^*], \quad F_2, F_3 \quad EG$$

$$u_1 \in [u_1^{\min}(N), u_{1F2}^*] \quad (DH).$$



4. (,)
 2013 .) (. .), (. .)

u_1 , F_2, F_3 :

$$u_1 > u_{1F3}^*,$$

$$(18) \quad u_1 = u_1^{\min}(N), \quad (38) \quad (15)-$$

2013 . 5,8 . .

6.

1. . . .
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THE OPTIMIZATION MODELS OF PRODUCTION CYCLES AT THE PLANTS OF BEARING INDUSTRY

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Abstract: The problem of optimization of inventory in the production process of enterprises of bearing industry is considered. Static and dynamic optimization models of production orders by the criterion of duration of a production cycle, taking into account the limitations imposed by functions of demand for the products and features suppliers of materials, as well as standards of production costs are developed. Analytical optimization mechanisms are formed, on the basis of which the simulation of production plans, order and delivery of materials in production is fulfilled.

Key words: production cycle, work in process, finished products, optimization, supply and demand, the ratio of production costs.

(5), (6):

[4]

$$(1) F_1(u) = \frac{T}{C(u)} \sum_{i=1}^3 \bar{u}_i, F_2(u) = F_1(u) + \frac{T}{R(u)} \bar{u}_4,$$

$$\bar{u}_i -$$

$$(2) \bar{u}_i = \frac{u_i^0 + u_i^T}{2}, i = 1, \dots, 4.$$

$$(3) u_1 = u_1^T - u_1^0 + u_2, u_2 = u_2^T - u_2^0 + u_3 - P,$$

$$u_3 = u_3^T - u_3^0 + C, u_4 = u_4^T - u_4^0 + g,$$

$$(4) \bar{u}_1 = u_1^0 + \frac{u_1 - u_2}{2}, \bar{u}_2 = u_2^0 + \frac{u_2 + P - u_3}{2},$$

$$\bar{u}_3 = u_3^0 + \frac{u_3 - C}{2}, \bar{u}_4 = u_4^0 + \frac{u_4 - g}{2},$$

$$u_i^T -$$

$$(5) R(u) = u_4.$$

(2), (4), (5) (1), (4), (5).

I: (8), (12)

(19)

$$(6) P_{\Sigma} = \sum_{j_1=1}^{J_1} A_{z_{j_1}} u_1^{r_{z_{j_1}}+1} + B_P \left(\sum_{j_1=1}^{J_1} u_{1j_1} \right)^{S_P},$$

(6),

(19)

$$P'_{\Sigma u_{1j_1}} = A_{z_{j_1}} (r_{z_{j_1}} + 1) u_1^{r_{z_{j_1}}} + B_P S_P \left(\sum_{j_1=1}^{J_1} u_{1j_1} \right)^{S_P-1} = 0,$$

$$j_1 = 1, \dots, J_1$$

(20).

(20)

$$(7) r_{z_{j_1}} < -1.$$

(8)

$$P''_{\Sigma u_{1j_1}} = A_{z_{j_1}} r_{z_{j_1}} (r_{z_{j_1}} + 1) u_1^{r_{z_{j_1}}-1} + B_P S_P (S_P - 1) \left(\sum_{j_1=1}^{J_1} u_{1j_1} \right)^{S_P-2} > 0,$$

$$j_1 = 1, \dots, J_1$$

$$\left\{ \begin{array}{l} S_P > 1 \cap B_P S_P (S_P - 1) \left(\sum_{j_1=1}^{J_1} u_{1j_1} \right)^{S_P-2} \geq \\ A_{z_{j_1}} |r_{z_{j_1}} + 1| r_{z_{j_1}} u_1^{r_{z_{j_1}}-1}, \forall r_{z_{j_1}} < 0, \\ S_P \leq 1 \cap r_{z_{j_1}} < -1 \cap A_{z_{j_1}} (r_{z_{j_1}} + 1) r_{z_{j_1}} u_1^{r_{z_{j_1}}-1} > \\ B_P S_P |S_P - 1| \left(\sum_{j_1=1}^{J_1} u_{1j_1} \right)^{S_P-2}, \end{array} \right.$$

,

(7),

(8)

(21).

2:

(5)

$$(9) \quad F'_{1u_1}(u_1) = -s_c \frac{T u_{\Sigma}^0}{B_c} u_1^{-s_c-1} + \frac{T}{2B_c} (1-s_c) u_1^{-s_c} + \frac{T B_p}{2B_c} (s_p - s_c) u_1^{s_p-s_c-1} = 0$$

(25)

u_{1F1}^*

(5)

$$F''_{1u_1}(u_1) = -s_c(-s_c-1) \frac{T u_{\Sigma}^0}{B_c} u_1^{-s_c-2} - \frac{T}{2B_c} (1-s_c) s_c u_1^{-s_c-1} +$$

$$\frac{T B_p}{2B_c} (s_p - s_c)(s_p - s_c - 1) u_1^{s_p-s_c-2} > 0$$

$$(10) \quad \frac{s_c [2(s_c + 1)u_{\Sigma}^0 + s_c - 1] u_1 + B_p (s_c - s_p)(s_c + 1 - s_p) u_1^{s_p}}{B_p (s_c - s_p)(s_c + 1 - s_p) u_1^{s_p}} > 0$$

$$u_{\Sigma}^0 \gg s_c, \quad 2(s_c + 1)u_{\Sigma}^0 + s_c \gg 1; \quad (10)$$

s_c, s_p .

$$s_c, s_p, \quad (8), (9), \quad (10)$$

$$(11) \quad \begin{cases} s_c > s_p \cup [s_c < s_p \cap s_c + 1 < s_p] \forall u_{1F1}^* \geq 0, \\ s_c < s_p \cap s_c + 1 > s_p \cap \{(s_c, s_p, u_{\Sigma}^0, u_1)\} > 0, \end{cases}$$

$$\begin{aligned} \{ (s_c, s_p, u_\Sigma^0, u_1) = s_c [2(s_c + 1)u_\Sigma^0 + s_c - 1] u_1 + \\ B_p |s_c - s_p| (s_c + 1 - s_p) u_1^{sp} \end{aligned} \quad (23) \quad (11) \quad (26).$$

3:

(6)

$$\begin{aligned} F'_{2u_1}(u_1) = -s_c \frac{T u_\Sigma^0}{B_c} u_1^{-s_c-1} + \frac{T}{2B_c} (1 - s_c) u_1^{-s_c} + \frac{T B_p}{2B_c} (s_p - s_c) u_1^{sp-s_c-1} - \\ - s_R \frac{T u_4^0}{B_R} u_1^{-s_R-1} - \frac{T B_g}{2B_R} (s_g - s_R) u_1^{s_g-s_R-1} = 0, \end{aligned}$$

$$\begin{aligned} - s_c \frac{u_\Sigma^0}{B_c} u_{1F2}^{*-s_c-1} + \frac{1 - s_c}{2B_c} u_{1F2}^{*-s_c} + \frac{B_p}{2B_c} (s_p - s_c) u_{1F2}^{*sp-s_c-1} - \\ s_R \frac{u_4^0}{B_R} u_{1F2}^{*-s_R-1} - \frac{B_g}{2B_R} (s_g - s_R) u_{1F2}^{*s_g-s_R-1} = 0 \end{aligned} \quad (32)$$

$$u_{1F2}^* \quad (6)$$

$$\begin{aligned} F''_{2u_1}(u_1) = s_c (s_c + 1) \frac{u_\Sigma^0}{B_c} u_1^{-s_c-2} + \frac{s_c (s_c - 1)}{2B_c} u_1^{-s_c-1} + \\ \frac{B_p}{2B_c} (s_p - s_c) (s_p - s_c - 1) u_1^{sp-s_c-2} + \\ + s_R (s_R + 1) \frac{u_4^0}{B_R} u_1^{-s_R-2} - \frac{B_g}{2B_R} (s_g - s_R) (s_g - s_R - 1) u_1^{s_g-s_R-2} > 0, \end{aligned}$$

$$(12) \quad \left\{ (s_C, s_P, u_\Sigma^0, u_{1F2}^*) + s_R(s_R + 1) \frac{u_4^0}{B_R} u_{1F2}^{*-s_R-2} + \frac{B_g}{2B_R} (s_g - s_R)(s_R + 1 - s_g) u_{1F2}^{*s_g - s_R - 2} > 0 \right.$$

(26)

$$(13) \quad \left\{ (s_C, s_P, u_\Sigma^0, u_{1F2}^*) > 0 \right.$$

(13)

(12)

$$(14)$$

u_{1F2}^*

$$\left\{ \begin{array}{l} (s_g > s_R \cap s_g > s_R + 1) \cap \left\{ (s_C, s_P, u_\Sigma^0, u_{1F2}^*) + s_R(s_R + 1) \frac{u_4^0}{B_R} u_{1F2}^{*-s_R-2} + \frac{B_g}{2B_R} (s_g - s_R)(s_R + 1 - s_g) u_{1F2}^{*s_g - s_R - 2} \geq 0, \right. \\ (s_g > s_R \cap s_g < s_R + 1) \forall u_{1F2}^*, \\ s_g \leq s_R \cap \left\{ (s_C, s_P, u_\Sigma^0, u_{1F2}^*) + s_R(s_R + 1) \frac{u_4^0}{B_R} u_{1F2}^{*-s_R-2} + \frac{B_g}{2B_R} (s_g - s_R)(s_R + 1 - s_g) u_{1F2}^{*s_g - s_R - 2} > 0. \right. \end{array} \right.$$

(24) (14)

(33).

4:

$$(15) \quad F_3(u_1) = B_R u_1^{s_R} - B_C u_1^{s_C},$$

$$(9), (10) \quad (7)$$

$$(16) \quad F'_{3u_1}(u_1) = B_R S_R u_1^{S_R-1} - B_C S_C u_1^{S_C-1} = 0, \quad (36).$$

$$(15) \quad F''_{3u_1}(u_1) = B_R (S_R - 1) S_R u_1^{S_R-2} - B_C (S_C - 1) S_C u_1^{S_C-2} < 0, \quad (37).$$

5:

$$(17) \quad L_k = F_k(u_1) + \lambda_{1k} (u_1^{\min}(N) - u_1) + \lambda_{2k} (u_1^{\max}(N) - u_1) + \lambda_{3k} (u_1^{\min}(z) - u_1), k = 1, 2, 3 \quad (18)$$

$$(18) \quad \frac{\partial L_k}{\partial u_1} = \frac{\partial F_k(u_1)}{\partial u_1} - \lambda_{1k} - \lambda_{2k} - \lambda_{3k} = 0,$$

$$(19) \quad \frac{\partial L_k}{\partial \lambda_{1k}} = u_1^{\min}(N) - u_1 \leq 0, \quad \frac{\partial L_k}{\partial \lambda_{2k}} = u_1^{\max}(N) - u_1 \geq 0, \quad \frac{\partial L_k}{\partial \lambda_{3k}} = u_1^{\min}(z) - u_1 \leq 0, k = 1, 2, 3$$

(19)

(18), (19)

$$\lambda_{1k} = \lambda_{2k} = \lambda_{3k} = 0,$$

(18)

$$\frac{\partial F_k(u_1)}{\partial u_1} = 0, k = 1, 2, 3,$$

(25), (32), (36)

$$u_{1Fk}^*, k = 1, 2, 3,$$

$$u_{1(k)}^* = u_{1Fk}^*, k = 1, 2, 3.$$

(19)

(18), (19)

$$(20) u_1 = u_1^{\min}(N) \cup u_1 = u_1^{\max}(N) \cup u_1 = u_1^{\min}(z),$$

(38).

(15)-(17)

(18)

(26), (33),

(37)

$$u_{1Fk}^* \in U .$$